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# GRADE 12 DIPLOMA EXAMINATION

Mathematics 30

June 1989



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# GRADE 12 DIPLOMA EXAMINATION MATHEMATICS 30

#### DESCRIPTION

Time: 21/2 hours

Total possible marks: 65

This is a CLOSED-BOOK examination consisting of three parts:

PART A: 45 multiple-choice questions each with a value of 1 mark.

PART B: Seven machine-scorable open-ended questions each with a value of 1 mark.

PART C: Three written-response questions for a total of 13 marks.

#### GENERAL INSTRUCTIONS

All numbers used in this examination are to be considered as EXACT numbers and are not the result of a measurement.

A tear-out formula and z-score sheet is included in the booklet.

All students are expected to provide their own approved scientific calculator.

NOTE: The perforated pages at the back of this booklet may be torn out and used for your rough work. NO MARKS will be given for work done on the tear-out sheets.

#### DO NOT FOLD EITHER THE ANSWER SHEET OR THE EXAMINATION BOOKLET

The presiding examiner will collect the answer sheet and examination booklet for transmission to Alberta Education.

JUNE 1989

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#### PART A

#### **INSTRUCTIONS**

C.

D.

Chemistry

Mathematics

There are 45 multiple-choice questions with a value of one mark each in this section of the examination. All numbers used in the questions are to be considered as EXACT numbers and are not the result of a measurement. Use the separate answer sheet provided and follow the specific instructions given.

Read each question carefully and decide which of the choices BEST completes the statement or answers the question. Locate that question number on the answer sheet and fill in the space that corresponds to your choice. USE AN HB PENCIL ONLY.

| Example                                     | Al | nswei | · Sne | et |  |
|---------------------------------------------|----|-------|-------|----|--|
| This examination is for the subject area of | Α  | В     | C     | D  |  |
| A. Biology B. Physics                       | ①  | 2     | 3     | •  |  |

If you wish to change an answer, please erase your first mark completely.

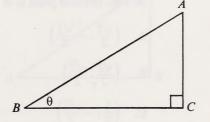
NOTE: The perforated pages at the back of this booklet may be torn out and used for your rough work. NO MARKS will be given for work done on the tear-out sheets.

WHEN YOU HAVE COMPLETED PART A, PROCEED DIRECTLY TO PART B

DO NOT TURN THE PAGE TO START THE EXAMINATION UNTIL TOLD TO DO SO BY THE PRESIDING EXAMINER

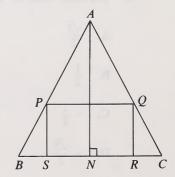
- iv -

- 1. In  $\triangle ABC$ , if  $\angle A = 37^{\circ}$ ,  $\angle B = 29^{\circ}$ , and c = 5.2 cm, then the value of b correct to the nearest tenth of a centimetre is
  - A. 4.2 cm
  - B. 3.4 cm
  - C. 2.8 cm
  - D. 1.3 cm
- 2. The exact value of  $\frac{\sin^2 45^\circ + \cos^2 45^\circ}{\sin 60^\circ \cos 30^\circ}$  is
  - **A.**  $\frac{3}{4}$
  - **B.**  $\frac{2\sqrt{3}}{3}$
  - C.  $\frac{4}{3}$
  - **D.**  $\frac{4\sqrt{2}}{3}$
- 3. In  $\triangle ABC$  shown at the right, BC = 12 cm and  $\tan \theta = \frac{2}{3}$ . The area of this triangle is
  - **A.** 36 cm<sup>2</sup>
  - **B.** 48 cm<sup>2</sup>
  - C. 72 cm<sup>2</sup>
  - D. 96 cm<sup>2</sup>

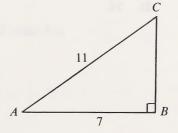


- 4. The exact value of  $\sin\left(\frac{11\pi}{3}\right)$  is
  - **A.**  $\frac{\sqrt{3}}{2}$
  - **B.**  $\frac{1}{2}$
  - C.  $-\frac{1}{2}$
  - **D.**  $-\frac{\sqrt{3}}{2}$

- 5. For  $180^{\circ} < \theta < 360^{\circ}$ , which of the primary trigonometric functions may have positive values?
  - tan  $\theta$  and  $\cos \theta$
  - $\tan \theta$  and  $\sin \theta$
  - C.  $\cos \theta$  and  $\sin \theta$
  - **D.**  $\cos \theta$  only
- Two airplanes leave the same airport in city A. One flies 75 km to city B and the other flies 245 km to city C. If the distance between B and C is 250 km, the angle between the flight paths of the airplanes correct to the nearest degree is
  - A. 80°
  - В. 85°
  - C. 95°
  - 100° D.
- 7. For the path of length  $\frac{-9\pi}{4}$  on a unit circle, if the initial point is at (1, 0), then the terminal point is at
  - **A.**  $\left(\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}\right)$
  - **B.**  $\left(\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right)$
  - C.  $\left(\frac{1}{2}, -\frac{\sqrt{3}}{2}\right)$
  - **D.**  $\left(\frac{1}{2}, \frac{\sqrt{3}}{2}\right)$
- **8.** In  $\triangle ABC$  shown at the right, AB = AC, BC = 8, and AN = 10. If SB = RC = y, then the area of the rectangle PQRS as a function of y is
  - **A.** y(4 y)
  - **B.** -2.5y(8 y)
  - C. 2.5y(8 + 2y)D. 2.5y(8 2y)

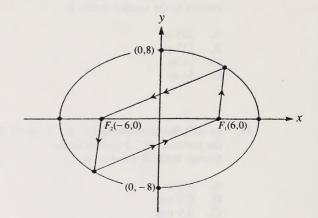


- 9. If  $4\cos^2\theta 7\cos\theta 2 = 0$ ,  $0^\circ < \theta \le 360^\circ$ , then the measure of  $\theta$  correct to the nearest degree is
  - **A.** 76°, 104°
  - **B.** 76°, 284°
  - C. 104°, 256°
  - **D.** 256°, 284°
- 10. A golfer is standing 350 m from a hole on a golf course. His first drive of 210 m is 15° to the right of the direct line to that hole. The remaining distance to the hole correct to the nearest metre is
  - A. 203 m
  - **B.** 157 m
  - C. 94 m
  - **D.** 54 m
- 11. In the triangle at the right, the measure of  $\angle A$  correct to the nearest tenth of a radian is
  - **A.** 0.6 rad
  - **B.** 0.7 rad
  - C. 0.9 rad
  - **D.** 1.1 rad



- 12. The centre of the circle  $x^2 + y^2 6y 6 = 0$  is at
  - **A.** (0, 3)
  - **B.** (3, 0)
  - C. (0, -3)
  - **D.** (-3, 0)
- 13. The focus of a parabola is at (-2, k) and the directrix is x 4 = 0. The vertex is at
  - **A.** (-8, k)
  - **B.** (-3, k)
  - C. (0, k)
  - **D.** (1, k)

- 14. An ellipse is defined by  $2x^2 + 6y^2 = p$ , and the major axis is 6 units long. The value of p is
  - **A.**  $\frac{2}{9}$
  - **B.**  $\frac{2}{3}$
  - **C**. 18
  - D. 54
- **15.** The perimeter of the parallelogram inscribed in the ellipse shown at the right is
  - **A.** 48
  - **B.** 40
  - C. 28
  - **D.** 14



- 16. The directrix of the parabola  $y^2 = 8(x + 2)$  is
  - **A.** x + 4 = 0
  - **B.** x + 6 = 0
  - **C.** x + 8 = 0**D.** x + 10 = 0
- 17. In an elliptical park, a fountain is located at one focus that is  $30\sqrt{3}$  m from the centre. If the maximum distance across the park is 120 m, then the minimum distance across the park through its centre is
  - **A.** 30 m
  - **B.** 60 m
  - C. 108 m
  - **D.** 119 m

18. The equation of a hyperbola whose conjugate axis is 8 units long and whose foci are at (-5, 0) and (5, 0) is

**A.** 
$$\frac{x^2}{9} - \frac{y^2}{16} = 1$$

**B.** 
$$\frac{x^2}{16} - \frac{y^2}{9} = -1$$

$$\mathbf{C.} \quad \frac{x^2}{39} - \frac{y^2}{64} = 1$$

$$\mathbf{D.} \quad \frac{x^2}{64} - \frac{y^2}{39} = -1$$

- 19. The midpoint of segment AE is at (3, 2). If A is at (-5, 4), then E is at
  - **A.** (-13, 6)
  - **B.** (-1, 3)
  - $\mathbf{C}$ . (4, -1)
  - **D.** (11, 0)
- **20.** The equation of a circle with centre (-1, -3) and radius 5 is

**A.** 
$$x^2 + y^2 + 2x + 6y + 5 = 0$$

**B.** 
$$x^2 + y^2 + 2x + 6y - 5 = 0$$

C. 
$$x^2 + y^2 - 2x - 6y - 15 = 0$$

**D.** 
$$x^2 + y^2 + 2x + 6y - 15 = 0$$

21. The asymptotes of the hyperbola  $4x^2 - 9y^2 = 36$  are

$$\mathbf{A.} \quad y = \pm \frac{9}{4}x$$

**B.** 
$$y = \pm \frac{3}{2}x$$

$$\mathbf{C.} \quad y = \pm \frac{2}{3}x$$

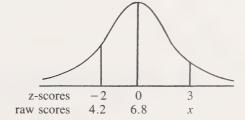
**D.** 
$$y = \pm \frac{4}{9}x$$

- 22. The locus of a set of points in a plane that are equidistant from a fixed point is
  - A. a circle
  - B. an ellipse
  - C. a parabola
  - D. a hyperbola
- 23. A parabola has a focus at (0, -16) and a directrix of y 16 = 0. The equation of this parabola is
  - **A.**  $x^2 = -16y$
  - **B.**  $y^2 = -16x$
  - C.  $x^2 = -64y$
  - **D.**  $y^2 = -64x$
- 24. The sum of all the integers between 21 and 150 that are divisible by 4 is
  - A. 2838
  - **B.** 2752
  - C. 2666
  - **D.** 2580
- 25. If the sum of the geometric series  $x + 3x + 9x + \dots + 3645$  is 5465, then the value of x is
  - **A.** 5
  - **B.** 4
  - **C.** 3
  - **D.** 2
- 26. Which of the following sequences is geometric?
  - A.  $\frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \ldots, \frac{n}{n+1}, \ldots$
  - **B.**  $-\frac{1}{2}, \frac{1}{3}, -\frac{1}{4}, \frac{1}{5}, \ldots, \frac{(-1)^n}{n+1}, \ldots$
  - C.  $\frac{2}{3}$ ,  $\frac{4}{5}$ ,  $\frac{8}{7}$ ,  $\frac{16}{9}$ , ...,  $\frac{2^n}{2n+1}$ , ...
  - **D.**  $\frac{2}{3}$ ,  $-\frac{2}{9}$ ,  $\frac{2}{27}$ ,  $-\frac{2}{81}$ , ...,  $(-1)^{n+1}(2)(\frac{1}{3})^n$ , ...

- 27. The limit of the sequence 15,  $7\frac{1}{2}$ , 5,  $3\frac{3}{4}$ , ...,  $\frac{15}{n}$ , ..., as  $n\to\infty$  is
  - A. nonexistent
  - **B.** 15
  - C. 1
  - **D.** 0
- **28.** The 10th term of the arithmetic sequence  $\frac{3}{4}$ ,  $\frac{5}{6}$ ,  $\frac{11}{12}$ , ... is
  - **A.**  $\frac{43}{4}$
  - **B.**  $\frac{5}{3}$
  - C.  $\frac{19}{12}$
  - **D.**  $\frac{3}{2}$
- **29.** The  $\lim_{n \to \infty} \left( \frac{3n^2 7n + 2}{4n} \right)$  is
  - A. nonexistent
  - **B.** 0
  - C.  $\frac{3}{4}$
  - **D.** 3
- 30. On a recent test, John and Pat scored 53% and 83% respectively. If the mean score of the test is 65% and John's z-score is -1.6, then Pat's z-score is
  - **A.** 1.6
  - **B.** 2.0
  - **C.** 2.4
  - **D.** 2.6

- 31. Standard deviation is a measure of dispersion of data about the
  - A. median
  - B. range
  - C. mean
  - D. mode
- 32. A certain population has a standard deviation of  $\sigma$  with a mean of  $\mu$ . Assuming a normal distribution, the percentage that lies within the interval between  $\mu 0.54\sigma$  and  $\mu 2.32\sigma$  is
  - A. 28.44%
  - **B.** 46.25%
  - C. 49.79%
  - **D.** 69.52%
- 33. A manufacturer of plastic earrings has determined that their masses are normally distributed with a mean of 12.4 g and a standard deviation of 2.0 g. If in a given week he makes 7500 earrings, how many will have a mass less than 11 g?
  - A. 1500
  - **B.** 1815
  - C. 1935
  - **D.** 2250
- **34.** A bag of marbles contains 30 black, 20 white, 20 red, and 30 blue marbles. What is the probability that, if one marble is chosen at random, it would NOT be black?
  - A.  $\frac{7}{8}$
  - **B.**  $\frac{7}{10}$
  - C.  $\frac{3}{8}$
  - **D.**  $\frac{3}{10}$

- 35. A breeder has determined that the mean life expectancy of her dogs is 10.3 a with a standard deviation of 1.7 a. If a normal distribution is assumed and Karen purchases one of these dogs, what is the probability that it will live longer than 6.9 a?
  - **A.** 0.4772
  - **B.** 0.6826
  - C. 0.9544
  - **D.** 0.9772
- **36.** The number of hours an infant sleeps per day is normally distributed with a mean of 13.2 h and a standard deviation of 1.6 h. The probability that an infant will sleep between 12.8 h and 15.6 h per day is
  - **A.** 0.1056
  - **B.** 0.3349
  - C. 0.3944
  - **D.** 0.5319
- **37.** The diagram at the right shows three z-scores and the corresponding raw scores. The value of x correct to the nearest tenth is
  - **A.** 8.1
  - **B.** 9.4
  - C. 10.7
  - **D.** 11.0



- **38.** Which of the following is equivalent to the equation  $\log_{10}(G) = 2 \log_{10}(M) \log_{10}(N)$ ?
  - $\mathbf{A.} \quad G = \frac{M^2}{N}$
  - **B.**  $G = \frac{2M}{N}$
  - $\mathbf{C.} \quad G = M^2 N$
  - $\mathbf{D.} \quad G = 2M N$

- **39.** The solution for the equation  $9^{2x} = \left(\frac{1}{3}\right)^{x+6}$  is
  - **A.** 6
  - **B.** 2
  - C.  $-\frac{4}{3}$
  - **D.**  $-\frac{6}{5}$
- **40.** When  $3x^4 x^2 + x 5$  is divided by x + 2, the quotient is
  - **A.**  $3x^3 + 6x^2 13x + 2$
  - **B.**  $3x^3 6x^2 + 11x 21$
  - C.  $3x^3 6x^2 13x 25$
  - **D.**  $3x^3 7x^2 + 15x 35$
- **41.** If the graph of a third-degree polynomial function passes through (1, 4) and has x-intercepts of 2 and -3 only, the function could be
  - A.  $y = x^3 x^2 8x + 12$
  - **B.**  $y = x^3 + x^2 6x + 8$
  - C.  $y = x^3 + 4x^2 3x 18$
  - **D.**  $y = x^3 4x^2 3x + 18$
- 42. A factored form of the polynomial  $(x^2 + x)^2 8(x^2 + x) + 12$  is
  - **A.** x(x + 1)(x 6)(x 2)
  - **B.** (x + 1)(x 2)(x + 2)(x + 3)
  - C. (x-1)(x-2)(x+2)(x+3)
  - **D.** (x-1)(x-2)(x+2)(x-3)

- **43.** The degree of the polynomial  $(x + 2)^3 + (x^3 + 1)^2 + 7x^5$  is
  - **A.** 5
  - **B.** 6
  - C. 10
  - **D.** 14
- **44.** If  $P(x) = 3x^2 ax + b$ , P(-1) = 14, and P(2) = 11, then the values of a and b respectively are
  - **A.** 6 and 5
  - **B.** 4 and 7
  - $\mathbf{C}$ . -4 and 15
  - **D.** -10 and 21
- **45.** The graph of  $P(x) = -3(2x + 3)(x^2 4)$  has x-intercepts of
  - **A.** 3, 4,  $-\frac{3}{2}$
  - **B.** 2, 3,  $\frac{3}{2}$
  - C.  $2, -2, -\frac{3}{2}$
  - **D.** 2, -2, 3,  $-\frac{3}{2}$

YOU HAVE NOW COMPLETED THE MULTIPLE-CHOICE SECTION OF THE EXAMINATION. PLEASE PROCEED TO PART B AND ANSWER THE MACHINE-SCORABLE OPEN-ENDED QUESTIONS.

#### PART B

#### INSTRUCTIONS

There are seven machine-scorable open-ended questions with a value of one mark each in this section of the examination. All numbers used in the questions are to be considered as EXACT numbers and are not the result of a measurement.

Read each question carefully.

Solve each question and write your answer correct to the nearest tenth.

Record your answer on the answer sheet by writing it in the boxes of the corresponding answer field and by filling in one circle in EVERY column.

### Sample Questions and Solutions

1. If  $\theta$  is acute and  $\sin \theta = 0.6735$ , then the measure of  $\theta$  correct to the nearest tenth of a degree is \_\_\_\_\_\_.

 $\theta = 42.33777464...$ 

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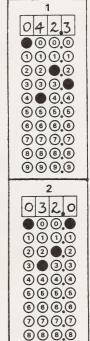
2. For the arithmetic series  $-8 + (-5) + (-2) + \dots + (85)$ , the number of terms correct to the nearest tenth is \_\_\_\_\_\_\_.

85 = -8 + (n - 1)(3)

93 = 3n - 3

n = 32

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9999

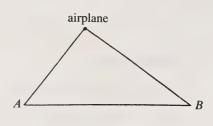
If you wish to change an answer, please erase your first mark completely.

NOTE: The perforated pages at the back of this booklet may be torn out and used for your rough work. NO MARKS will be given for work done on the tear-out sheets.

WHEN YOU HAVE COMPLETED PART B, PLEASE PROCEED DIRECTLY TO PART C.

1. At the same time, observers at A and B spot an airplane flying above and between them as shown in the diagram at the right.

The straight-line distance to the airplane is 9.4 km from A and 12.8 km from B. If the angle of elevation of the airplane is 53° from A, then the angle of elevation from B correct to the nearest tenth of a degree is \_\_\_\_\_\_.



2. For the hyperbola  $3x^2 - 8y^2 = 1$ , the length of the conjugate axis correct to the nearest tenth is \_\_\_\_\_\_.

3. If the point (-1, y) lies on the hyperbola  $\frac{y^2}{9} - \frac{4x^2}{3} = 1$ , then the positive value of y correct to the nearest tenth of a unit is \_\_\_\_\_\_.

4. The sum of the first six terms of the geometric series  $\frac{1}{8} + \frac{1}{2} + 2 + \dots$  correct to the nearest tenth is \_\_\_\_\_\_.

| The results of an achievement test were normally distributed. A student received a      |
|-----------------------------------------------------------------------------------------|
| raw score of 410 on the test for which the mean was 320 and the standard deviation      |
| was 60. If the results were translated to a normal distribution with a mean of 65 and   |
| a standard deviation of 12, then the student's score correct to the nearest tenth would |
| hacome                                                                                  |

6. If  $\log_n(a) = 3.6$  and  $\log_n(b) = 2.7$ , then  $\log_n(ab)$  correct to the nearest tenth is \_\_\_\_\_\_.

7. If 2 is a zero of the polynomial  $-2x^3 + kx^2 - 5x - 4$ , then the value of k correct to the nearest tenth of a unit is \_\_\_\_\_.

YOU HAVE NOW COMPLETED THE MACHINE-SCORABLE OPEN-ENDED SECTION OF THE EXAMINATION. PLEASE PROCEED TO PART C AND ANSWER THE WRITTEN-RESPONSE QUESTIONS.

#### PART C

#### INSTRUCTIONS

There are three written-response questions for a total of 13 marks in this section of the examination. All numbers used in the questions are to be considered as EXACT numbers and are not the result of a measurement.

Please write your answers in the examination booklet as neatly as possible.

Show all pertinent calculations and formulas.

NOTE: The perforated pages at the back of this booklet may be torn out and used for your rough work. NO MARKS will be given for work done on the tear-out sheets.

START PART C IMMEDIATELY



(5 marks)

- 1. For the series defined by  $\sum_{k=3}^{25} (4-2k)$ , find
  - a) the common difference

The common difference is

b) the sum of the series

The sum of the series is

2. Solve each of the following, correct to one decimal place.

$$\mathbf{a)} \quad \log_3(z) = \frac{2}{3}$$

The value of z is

**b)** 
$$\log_5(6) = y$$

The value of y is

$$c) \quad \log_x(8) = 4$$

The value of x is

#### FOR DEPARTMENT USE ONLY

(4 marks)

3. Prove the identity  $\frac{\sin^2 \theta}{1 - \cos \theta} = \frac{\sec \theta + 1}{\sec \theta}$  by expressing both the left side (L.S.) and the right side (R.S.) in terms of  $\cos \theta$ .

(ALL SUBSTITUTIONS AND PROCEDURES MUST BE SHOWN)

| L.S. | R.S. |
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YOU HAVE NOW COMPLETED THE EXAMINATION. IF YOU HAVE TIME, YOU MAY WISH TO GO BACK AND CHECK YOUR ANSWERS.

#### **MATHEMATICS 30** FORMULA SHEET

#### I. Trigonometry

1. 
$$\pi = 3.14159$$

$$2. \quad \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

3. 
$$a^2 = b^2 + c^2 - 2bc \cos A$$

4. 
$$\sin^2 A + \cos^2 A = 1$$

5. 
$$1 + \tan^2 A = \sec^2 A$$

$$6. \quad 1 + \cot^2 A = \csc^2 A$$

7. 
$$\sin\left(\frac{\pi}{2} - \theta\right) = \cos\theta$$

8. 
$$\cos\left(\frac{\pi}{2} - \theta\right) = \sin\theta$$

## II. Quadratic Relations

1. 
$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

2. 
$$d = \frac{|Ax_1 + By_1 + C|}{\sqrt{A^2 + B^2}}$$

3. 
$$M\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$$

4. 
$$(x - h)^2 + (y - k)^2 = r^2$$

5. 
$$x^2 + y^2 + Dx + Ey + F = 0$$

6. 
$$(y - k)^2 = 4p(x - h)$$

7. 
$$(x - h)^2 = 4p(y - k)$$

# III. Sequences, Series, and Limits

$$1. \quad t_n = a + (n-1)d$$

$$2. S_n = \frac{n(a + t_n)}{2}$$

3. 
$$S_n = \frac{n[2a + (n-1)d]}{2}$$

$$4. \quad A = P(1+i)^n$$

9. 
$$\sin(A + B) = \sin A \cos B + \cos A \sin B$$
  
10.  $\sin(A - B) = \sin A \cos B - \cos A \sin B$ 

10. 
$$\sin(A - B) = \sin A \cos B - \cos A \sin B$$

11. 
$$cos(A + B) = cos A cos B - sin A sin B$$

12. 
$$cos(A - B) = cos A cos B + sin A sin B$$

13. 
$$\sin(-\theta) = -\sin \theta$$

14. 
$$\cos(-\theta) = \cos \theta$$

15. 
$$tan(-\theta) = -tan \theta$$

1. 
$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$
 8.  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ ,  $a^2 = b^2 + c^2$ 

9. 
$$\frac{y^2}{a^2} + \frac{x^2}{b^2} = 1$$
,  $a^2 = b^2 + c^2$ 

10. 
$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$
,  $c^2 = a^2 + b^2$ 

11. 
$$\frac{y^2}{a^2} - \frac{x^2}{b^2} = 1$$
,  $c^2 = a^2 + b^2$ 

$$5. \quad t_n = ar^{n-1}$$

6. 
$$S_n = \frac{a(r^n - 1)}{r - 1}$$

$$7. \quad S_n = \frac{rt_n - a}{r - 1}$$

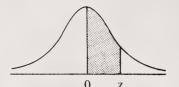
8. 
$$S = \frac{a}{1 - r}$$
,  $-1 < r < 1$ 

#### IV. Statistics

$$1. \quad \mu = \frac{x_1 + x_2 + \ldots + x_n}{n}$$

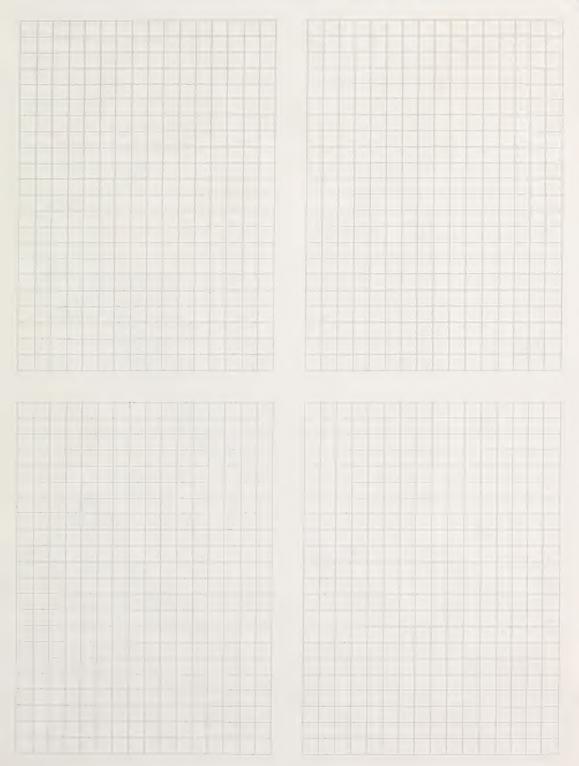
2. 
$$\sigma = \sqrt{\frac{(x_1 - \mu)^2 + \dots + (x_n - \mu)^2}{n}}$$

3. 
$$z = \frac{x - \mu}{\sigma}$$

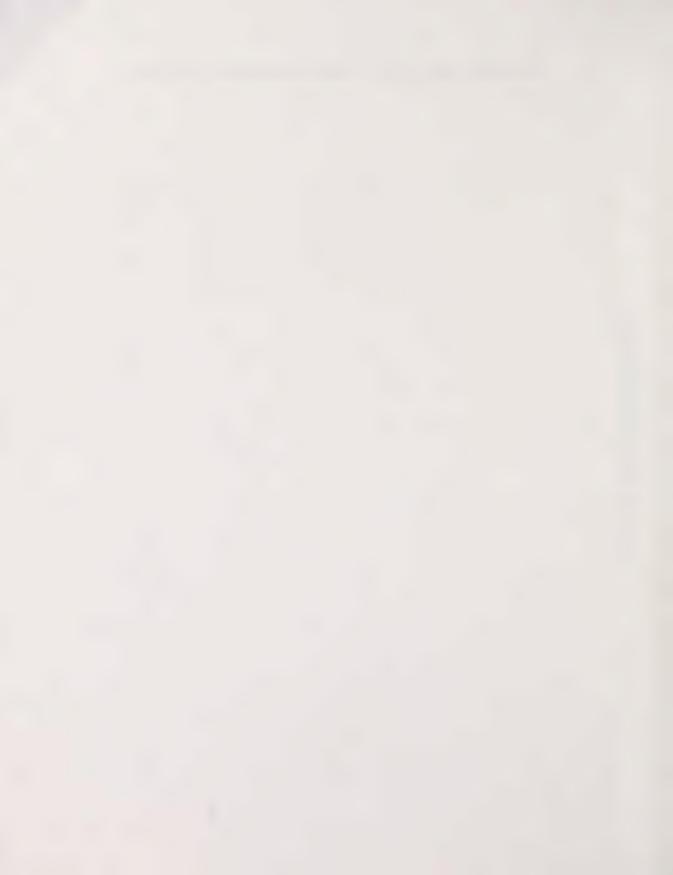


# AREAS UNDER THE STANDARD NORMAL CURVE

| Columb                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |     |        |        |        |        |        |        |        |        | 0 2    | Z      |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 0.1                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | Z   | 0      | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      |
| 0.1                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          |     |        |        |        |        |        |        |        |        |        |        |
| 0.2                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | 0.0 | 0.0000 | 0.0040 | 0.0080 | 0.0120 | 0.0160 | 0.0199 | 0.0239 | 0.0279 | 0.0319 | 0.0359 |
| 0.4                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | 0.1 | 0.0398 | 0.0438 | 0.0478 | 0.0517 | 0.0557 | 0.0596 | 0.0636 | 0.0675 | 0.0714 | 0.0754 |
| 0.4                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | 0.2 | 0.0793 | 0.0832 | 0.0871 | 0.0910 | 0.0948 | 0.0987 | 0.1026 | 0.1064 | 0.1103 | 0.1141 |
| 0.5         0.1915         0.1950         0.1985         0.2019         0.2054         0.2088         0.2123         0.2157         0.2190         0.2224           0.6         0.2258         0.2291         0.2324         0.2357         0.2389         0.2422         0.2454         0.2486         0.2518         0.2549           0.7         0.2580         0.2612         0.2642         0.2673         0.2704         0.2734         0.2764         0.2794         0.2823         0.2862           0.8         0.2881         0.2910         0.2939         0.2967         0.2996         0.3023         0.3051         0.3078         0.3106         0.3133           1.0         0.3413         0.3438         0.3461         0.3485         0.3508         0.3571         0.3577         0.3599         0.3389           1.1         0.3643         0.3665         0.3686         0.3788         0.3907         0.3925         0.3944         0.3577         0.3599         0.3810         0.3389           1.3         0.4032         0.4049         0.4066         0.4082         0.4099         0.4115         0.4131         0.4147         0.4162         0.4471           1.4         0.4192         0.4227                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | 0.3 | 0.1179 | 0.1217 | 0.1255 | 0.1293 | 0.1331 | 0.1368 | 0.1406 | 0.1443 | 0.1480 | 0.1517 |
| 0.6                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | 0.4 | 0.1554 | 0.1591 | 0.1628 | 0.1664 | 0.1700 | 0.1736 | 0.1772 | 0.1808 | 0.1844 | 0.1879 |
| 0.7         0.2580         0.2612         0.2642         0.2673         0.2704         0.2734         0.2794         0.2794         0.2794         0.2794         0.2823         0.2852           0.8         0.2881         0.2910         0.2939         0.2967         0.2996         0.3023         0.3051         0.3078         0.3166         0.3136         0.3212         0.3238         0.3664         0.3289         0.3315         0.3340         0.3365         0.3389           1.0         0.3413         0.3461         0.3485         0.3588         0.3578         0.3779         0.3770         0.3790         0.3810         0.3831           1.1         0.3643         0.3665         0.3686         0.3708         0.3779         0.3779         0.3790         0.3810         0.3831           1.2         0.3849         0.3889         0.3888         0.3907         0.3942         0.3944         0.3962         0.3990         0.3810         0.3830           1.2         0.3849         0.3889         0.3888         0.3907         0.3412         0.4171         0.4112         0.4113         0.4141         0.4162         0.4177           1.4         0.4421         0.4420         0.4422         0.4236 <td>0.5</td> <td>0.1915</td> <td>0.1950</td> <td>0.1985</td> <td>0.2019</td> <td>0.2054</td> <td>0.2088</td> <td>0.2123</td> <td>0.2157</td> <td>0.2190</td> <td>0.2224</td>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | 0.5 | 0.1915 | 0.1950 | 0.1985 | 0.2019 | 0.2054 | 0.2088 | 0.2123 | 0.2157 | 0.2190 | 0.2224 |
| 0.8                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | 0.6 | 0.2258 | 0.2291 | 0.2324 | 0.2357 | 0.2389 | 0.2422 | 0.2454 | 0.2486 | 0.2518 | 0.2549 |
| 0.9                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | 0.7 | 0.2580 | 0.2612 | 0.2642 | 0.2673 | 0.2704 | 0.2734 | 0.2764 | 0.2794 | 0.2823 | 0.2852 |
| 1.0                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | 0.8 | 0.2881 | 0.2910 | 0.2939 | 0.2967 | 0.2996 | 0.3023 | 0.3051 | 0.3078 | 0.3106 | 0.3133 |
| 1.1                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | 0.9 | 0.3159 | 0.3186 | 0.3212 | 0.3238 | 0.3264 | 0.3289 | 0.3315 | 0.3340 | 0.3365 | 0.3389 |
| 1.2                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | 1.0 | 0.3413 | 0.3438 | 0.3461 | 0.3485 | 0.3508 | 0.3531 | 0.3554 | 0.3577 | 0.3599 | 0.3621 |
| 1.3         0.4032         0.4049         0.4066         0.4082         0.4099         0.4115         0.4131         0.4147         0.4162         0.4306         0.4251         0.4265         0.4279         0.4292         0.4306         0.4319           1.5         0.4332         0.4345         0.4357         0.4370         0.4382         0.4394         0.4406         0.4418         0.4429         0.4441           1.6         0.4452         0.4463         0.4474         0.4484         0.4495         0.4505         0.4515         0.4525         0.4535         0.4545           1.7         0.4554         0.4664         0.4573         0.4582         0.4591         0.4608         0.4616         0.4625         0.4633           1.8         0.4641         0.4669         0.4666         0.4671         0.4678         0.4668         0.4693         0.4761         0.4761           2.0         0.4772         0.4778         0.4783         0.4788         0.4793         0.4788         0.4803         0.4808         0.4812         0.4817           2.1         0.4821         0.4826         0.4830         0.4834         0.4875         0.4876         0.4881         0.4848         0.4848         0.4848 <td>1.1</td> <td>0.3643</td> <td>0.3665</td> <td>0.3686</td> <td>0.3708</td> <td>0.3729</td> <td>0.3749</td> <td>0.3770</td> <td>0.3790</td> <td>0.3810</td> <td>0.3830</td>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | 1.1 | 0.3643 | 0.3665 | 0.3686 | 0.3708 | 0.3729 | 0.3749 | 0.3770 | 0.3790 | 0.3810 | 0.3830 |
| 1.4         0.4192         0.4207         0.4222         0.4236         0.4251         0.4265         0.4279         0.4292         0.4306         0.4319           1.5         0.4332         0.4345         0.4357         0.4370         0.4382         0.4394         0.4406         0.4418         0.4429         0.4441           1.6         0.4452         0.4463         0.4474         0.4484         0.4495         0.4505         0.4515         0.4525         0.4535         0.4545           1.7         0.4554         0.4564         0.4656         0.4664         0.4671         0.4688         0.4681         0.4625         0.4633           1.8         0.4641         0.4649         0.4656         0.4664         0.4671         0.4686         0.4693         0.4699         0.4706           1.9         0.47713         0.4778         0.4783         0.4788         0.4793         0.4780         0.4803         0.4808         0.4812         0.4817           2.0         0.4772         0.4778         0.4783         0.4788         0.4793         0.4780         0.4860         0.4812         0.4817           2.1         0.4821         0.4864         0.4868         0.4871         0.4875                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 1.2 | 0.3849 | 0.3869 | 0.3888 | 0.3907 | 0.3925 | 0.3944 | 0.3962 | 0.3980 | 0.3997 | 0.4015 |
| 1.5         0.4332         0.4345         0.4357         0.4370         0.4382         0.4394         0.4406         0.4418         0.4429         0.4441           1.6         0.4452         0.4463         0.4474         0.4484         0.4495         0.4505         0.4515         0.4525         0.4535         0.4545           1.7         0.4554         0.4564         0.4573         0.4582         0.4591         0.4599         0.4608         0.4616         0.4625         0.4633           1.8         0.4641         0.4649         0.4656         0.4664         0.4671         0.4678         0.4686         0.4699         0.4706           1.9         0.4713         0.4719         0.4726         0.4732         0.4738         0.4744         0.4750         0.4761         0.4767           2.0         0.4772         0.4778         0.4783         0.4788         0.4793         0.4798         0.4803         0.4808         0.4812         0.4817           2.1         0.4861         0.4864         0.4868         0.4871         0.4875         0.4878         0.4881         0.4884         0.4887         0.4889           2.3         0.4893         0.4868         0.4871         0.4967                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | 1.3 | 0.4032 | 0.4049 | 0.4066 | 0.4082 | 0.4099 | 0.4115 | 0.4131 | 0.4147 | 0.4162 | 0.4177 |
| 1.6         0.4452         0.4463         0.4474         0.4484         0.4495         0.4505         0.4515         0.4525         0.4535         0.4545           1.7         0.4554         0.4564         0.4573         0.4582         0.4591         0.4599         0.4608         0.4616         0.4625         0.4633           1.8         0.4641         0.4649         0.4656         0.4664         0.4671         0.4678         0.4686         0.4693         0.4699         0.4706           1.9         0.4713         0.4719         0.4726         0.4732         0.4738         0.4744         0.4750         0.4756         0.4761         0.4767           2.0         0.4772         0.4778         0.4783         0.4788         0.4793         0.4803         0.4808         0.4812         0.4817           2.1         0.4821         0.4826         0.4830         0.4834         0.4838         0.4842         0.4846         0.4887         0.4857           2.2         0.4861         0.4864         0.4868         0.4971         0.4975         0.4978         0.4881         0.4887         0.4887           2.3         0.4938         0.4940         0.4942         0.4925         0.4927                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | 1.4 | 0.4192 | 0.4207 | 0.4222 | 0.4236 | 0.4251 | 0.4265 | 0.4279 | 0.4292 | 0.4306 | 0.4319 |
| 1.7         0.4554         0.4564         0.4573         0.4582         0.4591         0.4599         0.4608         0.4616         0.4625         0.4633           1.8         0.4641         0.4649         0.4656         0.4664         0.4671         0.4678         0.4686         0.4693         0.4699         0.4706           1.9         0.4713         0.4719         0.4726         0.4732         0.4738         0.4744         0.4750         0.4756         0.4761         0.4767           2.0         0.4772         0.4778         0.4783         0.4788         0.4793         0.4798         0.4803         0.4808         0.4812         0.4817           2.1         0.4821         0.4826         0.4830         0.4834         0.4838         0.4842         0.4846         0.4854         0.4857           2.2         0.4861         0.4864         0.4868         0.4971         0.4875         0.4878         0.4881         0.4884         0.4887         0.4896           2.3         0.4893         0.4940         0.4922         0.4925         0.4927         0.4929         0.4931         0.4932         0.4934         0.4948           2.4         0.4938         0.4940         0.4941                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | 1.5 | 0.4332 | 0.4345 | 0.4357 | 0.4370 | 0.4382 | 0.4394 | 0.4406 | 0.4418 | 0.4429 | 0.4441 |
| 1.8         0.4641         0.4649         0.4656         0.4664         0.4671         0.4678         0.4686         0.4693         0.4699         0.4706           1.9         0.4713         0.4719         0.4726         0.4732         0.4738         0.4744         0.4750         0.4756         0.4761         0.4767           2.0         0.4772         0.4778         0.4783         0.4788         0.4798         0.4803         0.4808         0.4812         0.4817           2.1         0.4821         0.4826         0.4830         0.4834         0.4838         0.4842         0.4846         0.4854         0.4857           2.2         0.4861         0.4864         0.4868         0.4871         0.4875         0.4878         0.4881         0.4887         0.4887           2.4         0.4918         0.4920         0.4922         0.4925         0.4927         0.4929         0.4931         0.4932         0.4934         0.4934           2.5         0.4938         0.4940         0.4943         0.4945         0.4946         0.4948         0.4949         0.4951         0.4952           2.6         0.4933         0.4955         0.4956         0.4957         0.4957         0.4977                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | 1.6 | 0.4452 | 0.4463 | 0.4474 | 0.4484 | 0.4495 | 0.4505 | 0.4515 | 0.4525 | 0.4535 | 0.4545 |
| 1.9         0.4713         0.4719         0.4726         0.4732         0.4738         0.4744         0.4750         0.4756         0.4761         0.4767           2.0         0.4772         0.4778         0.4783         0.4788         0.4793         0.4803         0.4808         0.4812         0.4817           2.1         0.4821         0.4826         0.4830         0.4834         0.4875         0.4878         0.4846         0.4864         0.4867         0.4875           2.2         0.4861         0.4864         0.4888         0.4901         0.4904         0.4906         0.4909         0.4911         0.4913         0.4913         0.4913         0.4940         0.4922         0.4925         0.4927         0.4929         0.4931         0.4932         0.4934         0.4946         0.4948         0.49491         0.4943         0.4946         0.4948         0.49491         0.4946         0.4948         0.49493         0.4936         0.4962         0.4963         0.4964         0.4948         0.49494         0.4951         0.4952         0.4964         0.4948         0.49494         0.4951         0.4952         0.4963         0.4964         0.4962         0.4963         0.4964         0.4962         0.4963         0.496                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 1.7 | 0.4554 |        | 0.4573 | 0.4582 | 0.4591 | 0.4599 | 0.4608 | 0.4616 | 0.4625 | 0.4633 |
| 2.0         0.4772         0.4778         0.4783         0.4788         0.4793         0.4798         0.4803         0.4808         0.4812         0.4817           2.1         0.4821         0.4826         0.4830         0.4834         0.4838         0.4842         0.4846         0.4850         0.4854         0.4857           2.2         0.4861         0.4864         0.4868         0.4871         0.4875         0.4878         0.4881         0.4884         0.4887         0.4890           2.3         0.4893         0.4896         0.4898         0.4901         0.4904         0.4906         0.4909         0.4911         0.4913         0.4913         0.4922         0.4925         0.4927         0.4929         0.4931         0.4932         0.4934         0.4936           2.5         0.4938         0.4940         0.4941         0.4943         0.4945         0.4946         0.4948         0.4949         0.4951         0.4952           2.6         0.4953         0.4955         0.4956         0.4957         0.4959         0.4960         0.4948         0.49492         0.4963         0.4964           2.7         0.4965         0.4966         0.4967         0.4968         0.4969         0.4970 <th>1.8</th> <th>0.4641</th> <th>0.4649</th> <th>0.4656</th> <th>0.4664</th> <th>0.4671</th> <th>0.4678</th> <th>0.4686</th> <th>0.4693</th> <th>0.4699</th> <th>0.4706</th>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 1.8 | 0.4641 | 0.4649 | 0.4656 | 0.4664 | 0.4671 | 0.4678 | 0.4686 | 0.4693 | 0.4699 | 0.4706 |
| 2.1         0.4821         0.4826         0.4830         0.4834         0.4838         0.4842         0.4846         0.4850         0.4854         0.4857           2.2         0.4861         0.4864         0.4868         0.4871         0.4875         0.4878         0.4881         0.4884         0.4887         0.4890           2.3         0.4893         0.4896         0.4898         0.4901         0.4904         0.4906         0.4909         0.4911         0.4913         0.4916           2.4         0.4918         0.4920         0.4922         0.4925         0.4927         0.4929         0.4931         0.4932         0.4934         0.4936           2.5         0.4938         0.4940         0.4941         0.4943         0.4945         0.4946         0.4948         0.4949         0.4951         0.4952           2.6         0.4953         0.4955         0.4956         0.4957         0.4959         0.4960         0.4961         0.4962         0.4963         0.4964           2.7         0.4965         0.4967         0.4968         0.4969         0.4970         0.4971         0.4972         0.4973         0.4973         0.4973         0.4973         0.4974         0.4982         0.4982 <th>1.9</th> <th>0.4713</th> <th>0.4719</th> <th>0.4726</th> <th>0.4732</th> <th>0.4738</th> <th>0.4744</th> <th>0.4750</th> <th>0.4756</th> <th>0.4761</th> <th>0.4767</th>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | 1.9 | 0.4713 | 0.4719 | 0.4726 | 0.4732 | 0.4738 | 0.4744 | 0.4750 | 0.4756 | 0.4761 | 0.4767 |
| 2.2       0.4861       0.4864       0.4868       0.4871       0.4875       0.4878       0.4881       0.4884       0.4887       0.4890         2.3       0.4893       0.4896       0.4898       0.4901       0.4904       0.4906       0.4909       0.4911       0.4913       0.4916         2.4       0.4918       0.4920       0.4922       0.4925       0.4927       0.4929       0.4931       0.4932       0.4934       0.4936         2.5       0.4938       0.4940       0.4941       0.4943       0.4945       0.4946       0.4948       0.4949       0.4951       0.4952         2.6       0.4953       0.4955       0.4956       0.4957       0.4959       0.4960       0.4961       0.4962       0.4963       0.4964         2.7       0.4965       0.4966       0.4967       0.4968       0.4969       0.4970       0.4971       0.4972       0.4973       0.4973       0.4974         2.8       0.4974       0.4982       0.4982       0.4983       0.4984       0.4984       0.4985       0.4986       0.4986         3.0       0.4987       0.4987       0.4988       0.4988       0.4989       0.4999       0.4999       0.4999       0.4999                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | 2.0 | 0.4772 | 0.4778 | 0.4783 | 0.4788 | 0.4793 | 0.4798 | 0.4803 | 0.4808 | 0.4812 | 0.4817 |
| 2.3         0.4893         0.4896         0.4898         0.4901         0.4904         0.4906         0.4909         0.4911         0.4913         0.4916           2.4         0.4918         0.4920         0.4922         0.4925         0.4927         0.4929         0.4931         0.4932         0.4934         0.4936           2.5         0.4938         0.4940         0.4941         0.4943         0.4945         0.4946         0.4948         0.4949         0.4951         0.4952           2.6         0.4953         0.4955         0.4956         0.4957         0.4959         0.4960         0.4961         0.4962         0.4963         0.4964           2.7         0.4965         0.4967         0.4968         0.4969         0.4970         0.4971         0.4972         0.4973         0.4974           2.8         0.4974         0.4975         0.4976         0.4977         0.4977         0.4978         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4986         0.4986         0.4988         0.4988         0.4985         0.4985         0.4986         0.4986           3.0         0.4987         0.4987         0.4988         0.4988 <th>2.1</th> <th>0.4821</th> <th>0.4826</th> <th>0.4830</th> <th>0.4834</th> <th>0.4838</th> <th>0.4842</th> <th>0.4846</th> <th>0.4850</th> <th>0.4854</th> <th>0.4857</th>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | 2.1 | 0.4821 | 0.4826 | 0.4830 | 0.4834 | 0.4838 | 0.4842 | 0.4846 | 0.4850 | 0.4854 | 0.4857 |
| 2.4         0.4918         0.4920         0.4922         0.4925         0.4927         0.4929         0.4931         0.4932         0.4934         0.4936           2.5         0.4938         0.4940         0.4941         0.4943         0.4945         0.4946         0.4948         0.4949         0.4951         0.4952           2.6         0.4953         0.4955         0.4956         0.4957         0.4959         0.4960         0.4961         0.4962         0.4963         0.4964           2.7         0.4965         0.4966         0.4967         0.4968         0.4969         0.4970         0.4971         0.4972         0.4973         0.4974           2.8         0.4974         0.4975         0.4976         0.4977         0.4977         0.4978         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4986         0.4986         0.4988         0.4984         0.4985         0.4985         0.4986         0.4986         0.4986         0.4986         0.4986         0.4986         0.4986         0.4988         0.4989         0.4989         0.4989         0.4989         0.4989                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 2.2 | 0.4861 | 0.4864 | 0.4868 | 0.4871 | 0.4875 | 0.4878 | 0.4881 | 0.4884 | 0.4887 | 0.4890 |
| 2.5         0.4938         0.4940         0.4941         0.4943         0.4945         0.4946         0.4948         0.4949         0.4951         0.4952           2.6         0.4953         0.4955         0.4956         0.4957         0.4959         0.4960         0.4961         0.4962         0.4963         0.4964           2.7         0.4965         0.4966         0.4967         0.4968         0.4969         0.4970         0.4971         0.4972         0.4973         0.4974           2.8         0.4974         0.4975         0.4976         0.4977         0.4977         0.4978         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4980         0.4981           2.9         0.4981         0.4982         0.4982         0.4983         0.4984         0.4985         0.4985         0.4986         0.4986           3.0         0.4987         0.4987         0.4988         0.4988         0.4989         0.4989         0.4989         0.4989         0.4999         0.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | 2.3 | 0.4893 | 0.4896 | 0.4898 | 0.4901 | 0.4904 | 0.4906 | 0.4909 | 0.4911 | 0.4913 | 0.4916 |
| 2.6         0.4953         0.4955         0.4956         0.4957         0.4959         0.4960         0.4961         0.4962         0.4963         0.4964           2.7         0.4965         0.4966         0.4967         0.4968         0.4969         0.4970         0.4971         0.4972         0.4973         0.4974           2.8         0.4974         0.4975         0.4976         0.4977         0.4977         0.4978         0.4979         0.4979         0.4980         0.4981           2.9         0.4981         0.4982         0.4982         0.4983         0.4984         0.4984         0.4985         0.4985         0.4986         0.4986           3.0         0.4987         0.4987         0.4987         0.4988         0.4988         0.4989         0.4989         0.4989         0.4989         0.4999         0.4990         0.4990         0.4990           3.1         0.4990         0.4991         0.4991         0.4992         0.4992         0.4992         0.4992         0.4992         0.4992         0.4993         0.4993         0.4993           3.2         0.4993         0.4995         0.4995         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996 <td>2.4</td> <td>0.4918</td> <td>0.4920</td> <td>0.4922</td> <td>0.4925</td> <td>0.4927</td> <td>0.4929</td> <td>0.4931</td> <td>0.4932</td> <td>0.4934</td> <td>0.4936</td>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | 2.4 | 0.4918 | 0.4920 | 0.4922 | 0.4925 | 0.4927 | 0.4929 | 0.4931 | 0.4932 | 0.4934 | 0.4936 |
| 2.7         0.4965         0.4966         0.4967         0.4968         0.4969         0.4970         0.4971         0.4972         0.4973         0.4974           2.8         0.4974         0.4975         0.4976         0.4977         0.4977         0.4978         0.4979         0.4979         0.4980         0.4981           2.9         0.4981         0.4982         0.4982         0.4983         0.4984         0.4984         0.4985         0.4985         0.4986         0.4986           3.0         0.4987         0.4987         0.4987         0.4987         0.4988         0.4988         0.4989         0.4989         0.4989         0.4989         0.4999         0.4992         0.4992         0.4992         0.4992         0.4992         0.4992         0.4993         0.4993         0.4993         0.4993         0.4993         0.4993         0.4993         0.4993         0.4994         0.4994         0.4994         0.4994         0.4994         0.4994         0.4994         0.4994         0.4994         0.4994         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997 <th>2.5</th> <th>0.4938</th> <th>0.4940</th> <th>0.4941</th> <th>0.4943</th> <th>0.4945</th> <th>0.4946</th> <th>0.4948</th> <th>0.4949</th> <th>0.4951</th> <th>0.4952</th>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 2.5 | 0.4938 | 0.4940 | 0.4941 | 0.4943 | 0.4945 | 0.4946 | 0.4948 | 0.4949 | 0.4951 | 0.4952 |
| 2.8         0.4974         0.4975         0.4976         0.4977         0.4977         0.4978         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4979         0.4980         0.4981           2.9         0.4981         0.4982         0.4982         0.4983         0.4984         0.4984         0.4985         0.4985         0.4986         0.4986           3.0         0.4987         0.4987         0.4987         0.4988         0.4988         0.4989         0.4989         0.4989         0.4989         0.4989         0.4999         0.4990         0.4990           3.1         0.4990         0.4991         0.4991         0.4991         0.4992         0.4992         0.4992         0.4992         0.4992         0.4993         0.4993         0.4993           3.2         0.4993         0.4994         0.4994         0.4994         0.4994         0.4994         0.4994         0.4994         0.4994         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 2.6 | 1      | 0.4955 | 0.4956 | 0.4957 | 0.4959 | 0.4960 | 0.4961 | 0.4962 | 0.4963 | 0.4964 |
| 2.9       0.4981       0.4982       0.4982       0.4983       0.4984       0.4984       0.4985       0.4985       0.4986       0.4986       0.4986         3.0       0.4987       0.4987       0.4987       0.4988       0.4988       0.4989       0.4989       0.4989       0.4989       0.4989       0.4999       0.4990       0.4990       0.4990       0.4990       0.4993       0.4993       0.4991       0.4991       0.4992       0.4992       0.4992       0.4992       0.4992       0.4992       0.4993       0.4993       0.4993       0.4993       0.4994       0.4994       0.4994       0.4994       0.4994       0.4994       0.4994       0.4994       0.4994       0.4994       0.4994       0.4994       0.4994       0.4994       0.4994       0.4994       0.4995       0.4995       0.4995       0.4995       0.4995       0.4995       0.4996       0.4996       0.4996       0.4996       0.4996       0.4996       0.4996       0.4996       0.4997       0.4997       0.4997       0.4997       0.4997       0.4997       0.4997       0.4997       0.4997       0.4997       0.4998       0.4998       0.4998       0.4998       0.4998       0.4998       0.4998       0.4998       0.4999                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         | 2.7 | 0.4965 | 0.4966 | 0.4967 | 0.4968 | 0.4969 | 0.4970 | 0.4971 | 0.4972 | 0.4973 | 0.4974 |
| 3.0         0.4987         0.4987         0.4987         0.4988         0.4988         0.4989         0.4989         0.4989         0.4989         0.4989         0.4989         0.4989         0.4989         0.4989         0.4989         0.4989         0.4989         0.4989         0.4989         0.4989         0.4989         0.4989         0.4989         0.4989         0.4989         0.4989         0.4989         0.4999         0.4992         0.4992         0.4992         0.4992         0.4992         0.4992         0.4992         0.4992         0.4992         0.4992         0.4992         0.4992         0.4992         0.4992         0.4992         0.4992         0.4992         0.4992         0.4992         0.4992         0.4992         0.4993         0.4993         0.4993         0.4993         0.4993         0.4993         0.4993         0.4995         0.4995         0.4995         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997         0.4998         0.4998         0.4998         0.4998         0.4998         0.4998 <td>2.8</td> <td>0.4974</td> <td>0.4975</td> <td>0.4976</td> <td>0.4977</td> <td>0.4977</td> <td>0.4978</td> <td>0.4979</td> <td>0.4979</td> <td>0.4980</td> <td>0.4981</td>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | 2.8 | 0.4974 | 0.4975 | 0.4976 | 0.4977 | 0.4977 | 0.4978 | 0.4979 | 0.4979 | 0.4980 | 0.4981 |
| 3.1         0.4990         0.4991         0.4991         0.4991         0.4992         0.4992         0.4992         0.4992         0.4992         0.4993         0.4993         0.4993         0.4994         0.4994         0.4994         0.4994         0.4994         0.4994         0.4994         0.4994         0.4994         0.4994         0.4995         0.4995         0.4995         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4996         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997         0.4997         0.4998         0.4998         0.4998         0.4998         0.4998         0.4998         0.4998         0.4998         0.4998         0.4998         0.4998         0.4998         0.4998         0.4999         0.4999         0.4999         0.4999         0.4999         0.4999         0.4999         0.4999         0.4999         0.4999         0.4999         0.4999         0.4999         0.4999         0.4999         0.4999         0.4999         0.4999         0.4999 <td>2.9</td> <td>0.4981</td> <td>0.4982</td> <td>0.4982</td> <td>0.4983</td> <td>0.4984</td> <td>0.4984</td> <td>0.4985</td> <td>0.4985</td> <td>0.4986</td> <td>0.4986</td>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | 2.9 | 0.4981 | 0.4982 | 0.4982 | 0.4983 | 0.4984 | 0.4984 | 0.4985 | 0.4985 | 0.4986 | 0.4986 |
| 3.2     0.4993     0.4994     0.4994     0.4994     0.4994     0.4994     0.4994     0.4994     0.4994     0.4994     0.4994     0.4994     0.4995     0.4995     0.4995     0.4995     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4997     0.4997     0.4997     0.4997     0.4997     0.4997     0.4997     0.4997     0.4997     0.4997     0.4997     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | 1   | 1      | 1      |        |        |        |        |        |        | 1      |        |
| 3.3     0.4995     0.4995     0.4995     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4996     0.4997     0.4997     0.4997     0.4997     0.4997     0.4997     0.4997     0.4997     0.4997     0.4998       3.5     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 1   | 1      | 1      |        | 1      |        | 1      |        |        |        |        |
| 3.4     0.4997     0.4997     0.4997     0.4997     0.4997     0.4997     0.4997     0.4997     0.4997     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | 1   |        |        |        |        |        | ŀ      |        |        |        |        |
| 3.5     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4998     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | 1   | 1      |        |        | 1      |        |        |        |        | 1      |        |
| 3.6     0.4998     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999     0.4999                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | 3.4 | 0.4997 | 0.4997 | 0.4997 | 0.4997 | 0.4997 | 0.4997 | 0.4997 | 0.4997 | 0.4997 | 0.4998 |
| 3.7   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.49 |     |        |        |        |        |        |        | 1      |        |        |        |
| 3.8   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999   0.4999                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 1   |        | 1      |        |        |        | l      | 1      |        |        |        |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 1   | 1      | 1      | 1      |        |        |        | 1      |        | 1      |        |
| 3.9   0.5000   0.5000   0.5000   0.5000   0.5000   0.5000   0.5000   0.5000   0.5000   0.5000   0.5000                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |     | 1      | 1      |        |        |        |        |        |        |        |        |
|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 3.9 | 0.5000 | 0.5000 | 0.5000 | 0.5000 | 0.5000 | 0.5000 | 0.5000 | 0.5000 | 0.5000 | 0.5000 |

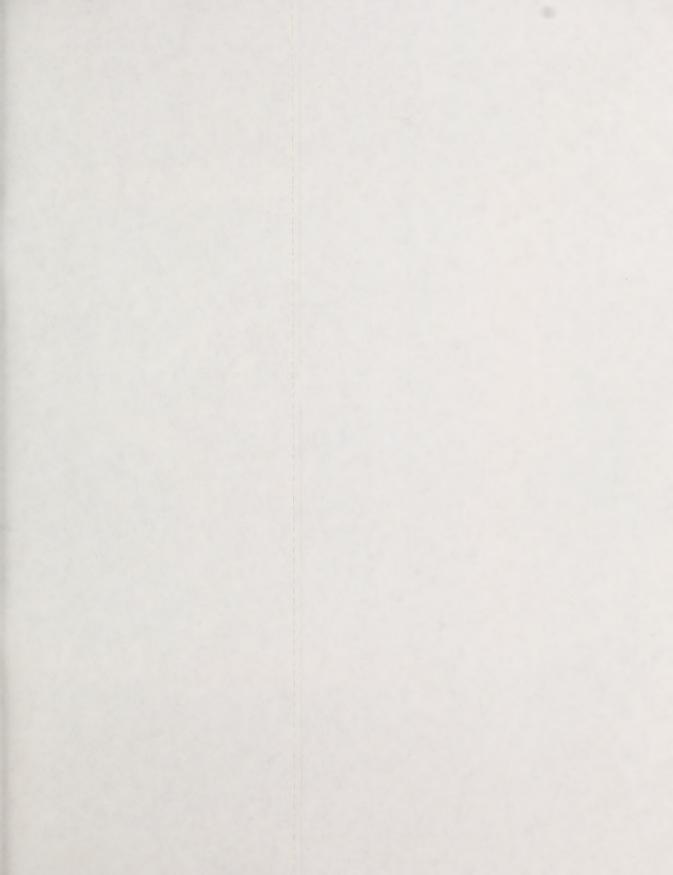












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